## 

Multi-Resource Fairness for Correlated and Elastic Demands

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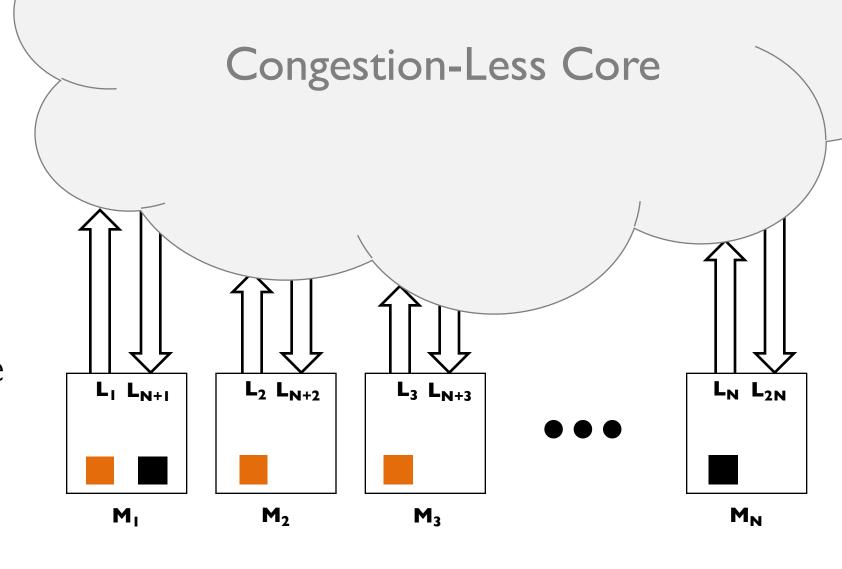






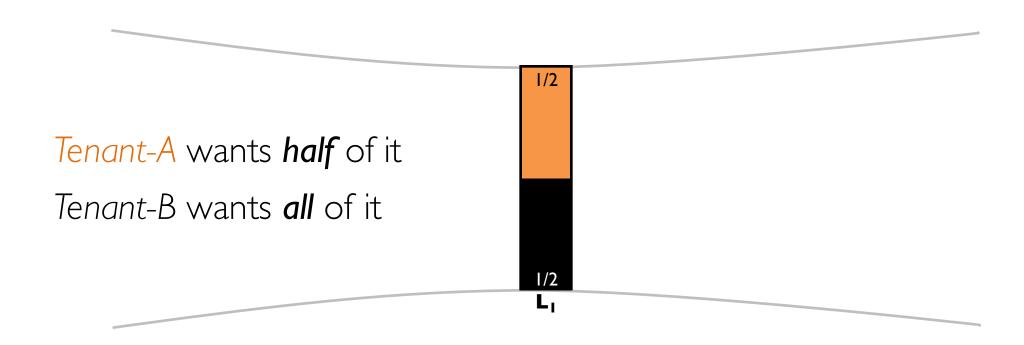
#### How to share the links between multiple tenants to provide

- I. optimal performance guarantees and
- 2. maximize utilization?





### Single-Resource Max-Min Fairness



#### 1. Optimal Isolation Guarantee

### Single-Resource Max-Min Fairness

Tenant-A wants half of it
Tenant-B wants all of it



**Progress (M)** of a tenant is its demand-normalized allocation

**Isolation Guarantee** is the minimum progress across all

#### Single-Resource Max-Min Fairness

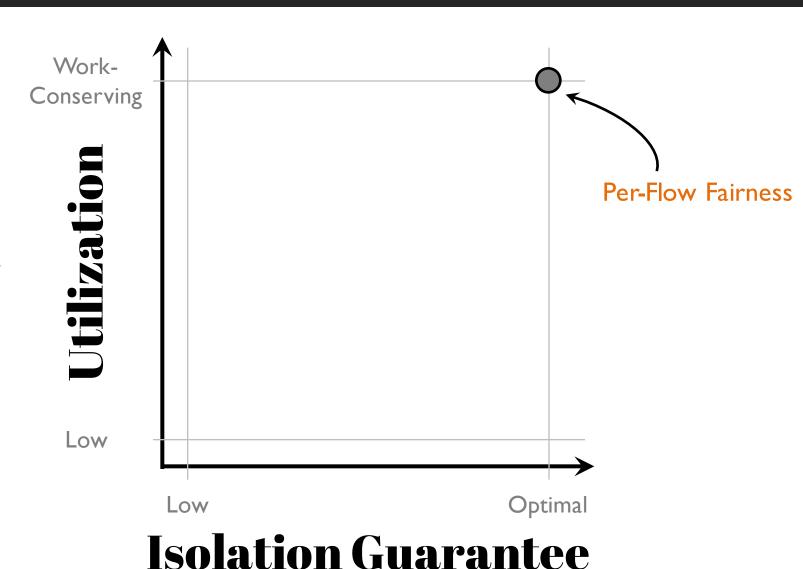
Tenant-A wants half of it
Tenant-B wants all of it



# Optimal Isolation Guarantee Work Conservation

### No Tradeoff for Single Resource

- 1. Optimal Isolation Guarantee
- 2. Work Conservation
- 3. Strategyproof



## Congestion-Less Core $L_2$ $L_{N+2}$ $L_3$ $L_{N+3}$ $L_{I}$ $L_{N+I}$ $L_N$ $L_{2N}$

 $M_3$ 

#### Tenants have different

I. placements,

2. communication patterns,

 $M_{I}$ 

 $M_2$ 

3. demand correlations,

4. ..

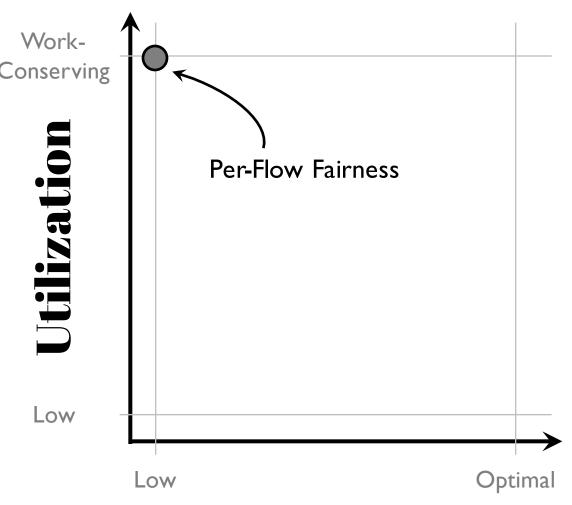


 $M_N$ 

#### Per-Flow Fairness For Multiple Resources

#### Low

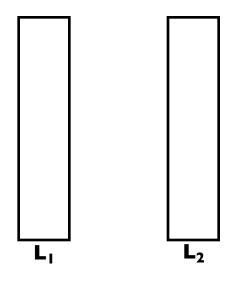
- 1. Optimal Isolation Guarantee
- 2. Work Conservation
- 3. Strategyproof



**Isolation Guarantee** 

#### Elastic Demands<sup>1</sup>

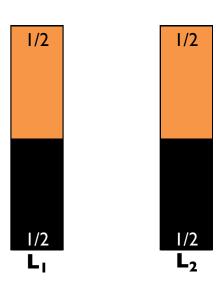
Tenant-A wants **all** of  $L_1$  and **all** of  $L_2$ 



Tenant-B wants **all** of  $L_1$  and **all** of  $L_2$ 

## Tenant-Level Max-Min Fairness (PS-P)

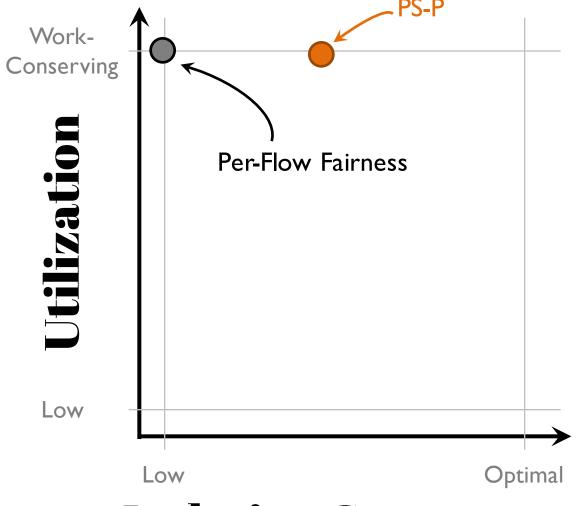
Tenant-A wants **all** of  $L_1$  and **all** of  $L_2$ 



Tenant-B wants **all** of  $L_1$  and **all** of  $L_2$ 

## Tenant-Level Max-Min Fairness (PS-P)

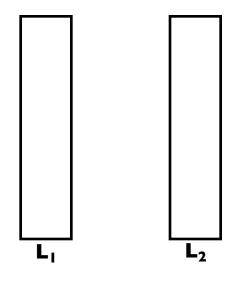
- 1. Suboptimal Isolation Guarantee
- 2. Work Conservation



**Isolation Guarantee** 

#### Correlated Demands

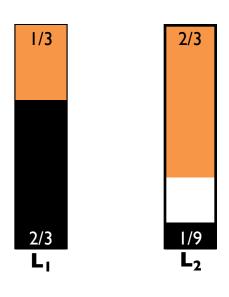
Tenant-A wants some of  $L_1$  and all of  $L_2$ 



Tenant-B wants **some** of  $L_2$  and **all** of  $L_1$ 

### Dominant Resource Fairness (DRF)

Tenant-A wants exactly half unit of  $L_1$  for each of  $L_2$ 



Tenant-B wants **exactly** 1/6 unit of  $L_2$  for **each** of  $L_1$ 

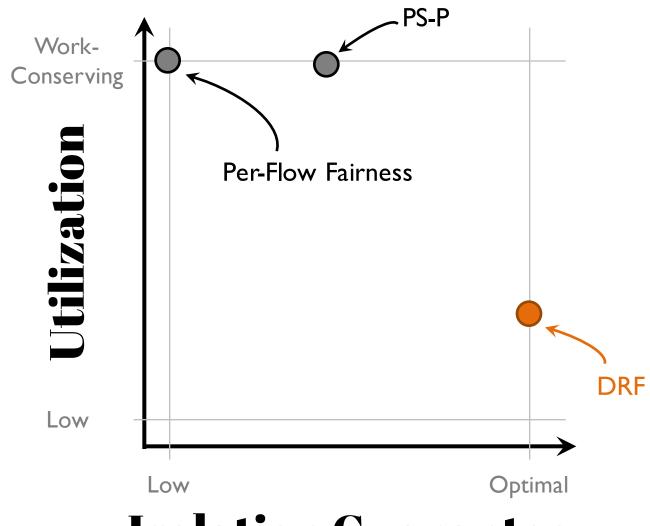
$$\mathbf{d_{A}} = \langle 1/2, 1 \rangle \quad \mathbf{a_{A}} = \langle 1/3, 2/3 \rangle \quad \mathbf{M_{A}} = \min\left(\frac{\mathbf{a_{A}^{i}}}{\mathbf{d_{A}^{i}}}\right) = 2/3$$

$$\mathbf{d_{B}} = \langle 1, 1/6 \rangle \quad \mathbf{a_{B}} = \langle 2/3, 1/9 \rangle \quad \mathbf{M_{B}} = \min\left(\frac{\mathbf{a_{B}^{i}}}{\mathbf{d_{B}^{i}}}\right) = 2/3$$

$$\mathbf{Min(M_{A}, M_{B})} = 2/3$$

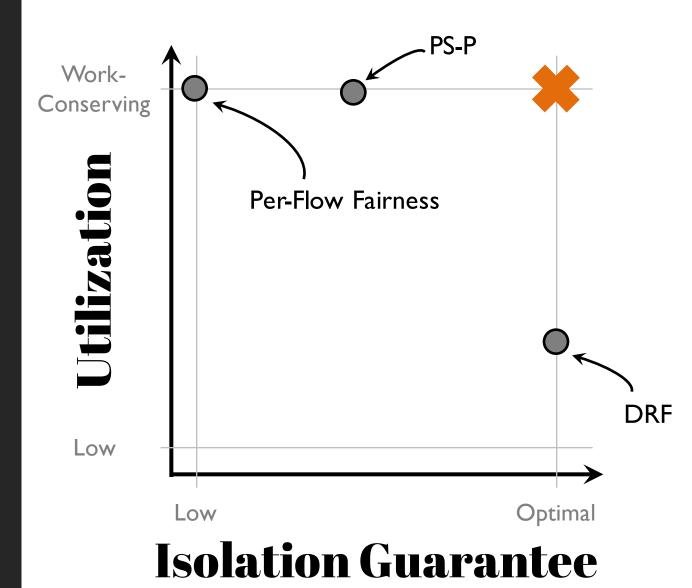
### Dominant Resource Fairness (DRF)

- 1. Optimal Isolation Guarantee
- 2. Arbitrarily Low Utilization
- 3. Strategyproof



**Isolation Guarantee** 

For elastic and correlated demands, can we simultaneously achieve optimal isolation guarantee and maximum utilization?



For elastic and correlated demands, can we simultaneously achieve optimal isolation guarantee and maximum utilization?



1. Why not?

2. What's the best we can achieve?

3. How can we achieve that?

4. Does it matter?

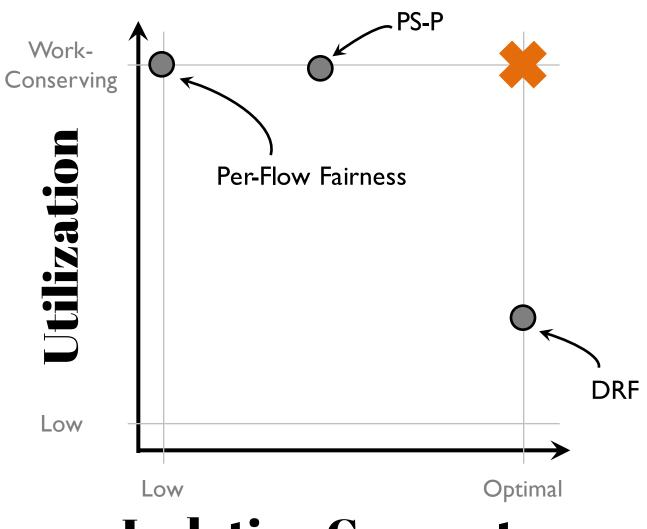


1. Why not?

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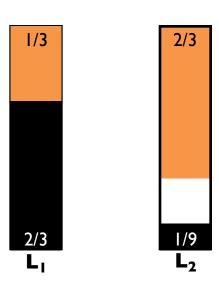
4. Does it matter?



**Isolation Guarantee** 

#### Elastic and Correlated Demands

Tenant-A wants at least half unit of  $L_1$  for each of  $L_2$ 



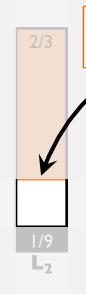
Tenant-B wants at least 1/6 unit of  $L_2$  for each of  $L_1$ 

$$d_A = \langle 1/2, 1 \rangle$$
  $a_A = \langle 1/3, 2/3 \rangle$   $M_A = 2/3$   
 $d_B = \langle 1, 1/6 \rangle$   $a_B = \langle 2/3, 1/9 \rangle$   $M_B = 2/3$   $M_B = 2/3$ 

#### Elastic and Correlated Demands

Tenant-A wants at least half unit of  $L_1$  for each of  $L_2$ 





#### Who gets this?

Tenant-B wants at least 1/6 unit of L<sub>2</sub> for each of L<sub>1</sub>

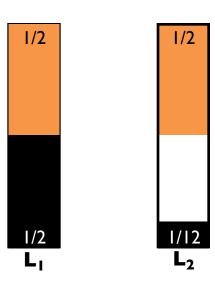
$$\mathbf{d_A} = \langle 1/2, 1 \rangle \quad \mathbf{d_A} = \langle 1/3, 2/3 \rangle \quad \mathbf{M_A} = 2/3$$

$$d_B = \langle 1, 1/6 \rangle$$
  $d_B = \langle 2/3, 1/9 \rangle$   $M_B = 2/3$ 

$$Min(M_A, M_B) = 2/3$$

#### Work Conservation Doesn't Work!

Tenant-A **lies** and asks for **one** unit of  $L_1$  for **each** of  $L_2$ 



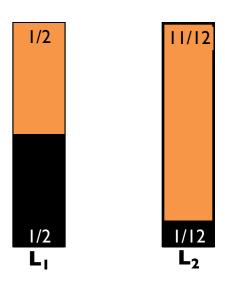
Tenant-B wants at least 1/6 unit of  $L_2$  for each of  $L_1$ 

$$d'_A = \langle |, | \rangle$$
  $a'_A = \langle |/_2, |/_2 \rangle$ 

$$\mathbf{d_B} = \langle 1, 1/6 \rangle$$
  $\mathbf{d_B} = \langle 1/2, 1/12 \rangle$ 

#### Work Conservation Doesn't Work!

Tenant-A **lies** and asks for **one** unit of  $L_1$  for **each** of  $L_2$ 



Tenant-B wants at least 1/6 unit of  $L_2$  for each of  $L_1$ 

$$\mathbf{d''_A} = \langle |, | \rangle$$
  $\mathbf{a''_A} = \langle |/_2, |/_2 \rangle$   $\mathbf{a''_A} = \langle |/_2, | |/| | 2 \rangle$   $\mathbf{M''_A} = | |//| 2$ 

$$\mathbf{d_B} = \langle |, |/6 \rangle \quad \mathbf{a_B} = \langle |/_2, |/| | 2 \rangle$$
  $\mathbf{M''_B} = |/2$ 

#### Prisoner's Dilemma

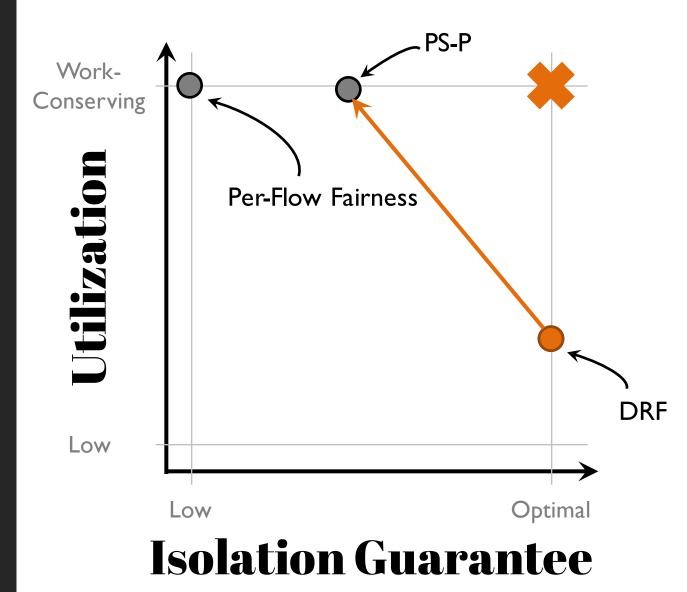
Doesn't Lie Lies

Doesn't Lie 
$$\frac{2}{3}$$
,  $\frac{2}{3}$   $\longrightarrow$   $\frac{11}{12}$ ,  $\frac{1}{2}$ 

Lies  $\frac{1}{2}$ ,  $\frac{3}{4}$   $\longrightarrow$   $\frac{1}{2}$ ,  $\frac{1}{2}$ 

#### 1. Why not?

Optimal isolation guarantee depends on being strategyproof, but work conservation cannot coexist with strategyproof-ness

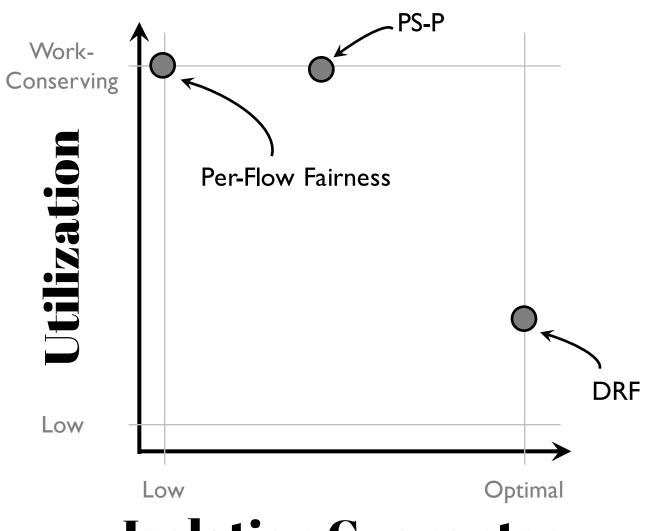


1. Why not?

2. What's the best we can achieve?

3. How can we achieve that?

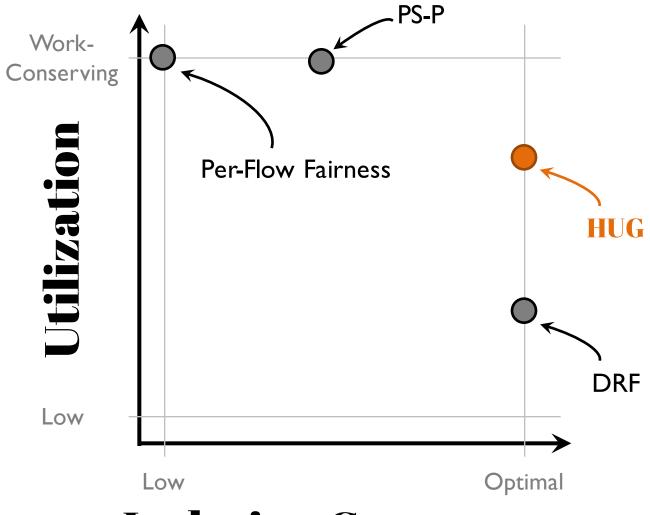
4. Does it matter?



**Isolation Guarantee** 

## HUG in Non-Cooperative Setting

- 1. Optimal Isolation Guarantee
- 2. Highest Utilization
- 3. Strategyproof



**Isolation Guarantee** 

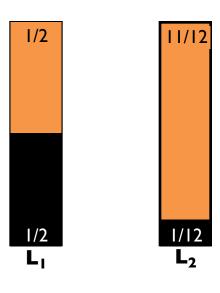


# Highest Utilization with the Optimal Isolation Guarantee

Restrict a tenant's allocation in any link to its allocation in the bottleneck link

#### Tenant-A Lied

Tenant-A **lies** and asks for **one** unit of  $L_1$  for **each** of  $L_2$ 

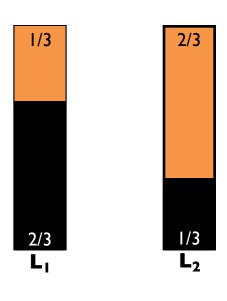


Tenant-B wants at least 1/6 unit of  $L_2$  for each of  $L_1$ 

$$\mathbf{d''_A} = \langle |, | \rangle$$
  $\mathbf{a''_A} = \langle |/_2, |/_2 \rangle$   $\mathbf{a''_A} = \langle |/_2, | |/| | 2 \rangle$   $\mathbf{M''_A} = |/_2$   
 $\mathbf{d_B} = \langle |, |/_6 \rangle$   $\mathbf{a_B} = \langle |/_2, |/| | 2 \rangle$   $\mathbf{M''_B} = |/_2$ 

### Everyone is Forced to Tell the Truth

Tenant-A wants at least half unit of L<sub>1</sub> for each of  $L_2$ 



Tenant-B wants at least 1/6 unit of L<sub>2</sub> for each of L<sub>I</sub>

$$d_A = < 1/2, 1> a_A = < 1/3, 2/3>$$

$$M_A = 2/3$$

$$d_B = \langle 1, 1/6 \rangle$$
  $d_B = \langle 2/3, 1/9 \rangle$   $d_B'' = \langle 2/3, 1/3 \rangle$   $M_B = 2/3$ 

$$a''_{B} = <2/3, 1/3>$$

$$M_B = 2/3$$



# Highest Utilization with the Optimal Isolation Guarantee

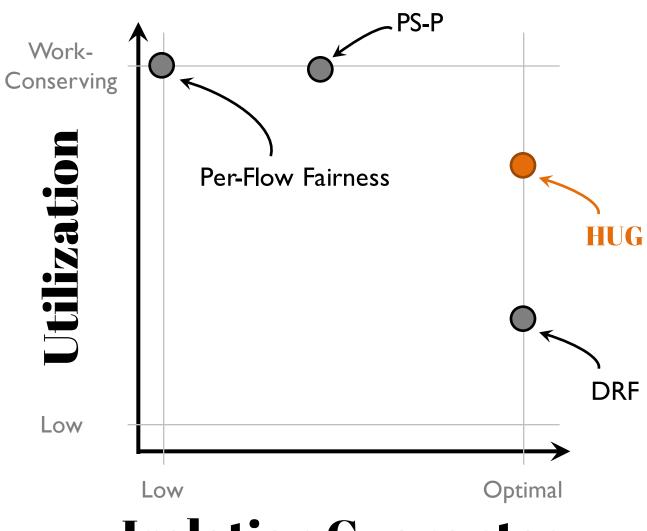
- 1. Tenants update correlation vectors through an API
- 2. Operators calculate HUG centrally and enforce it locally

1. Why not?

2. What's the best we can achieve?

3. How can we achieve that?

4. Does it matter?

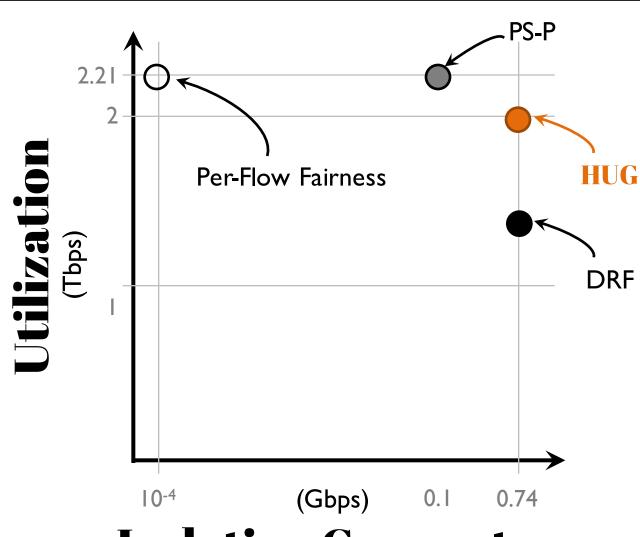


**Isolation Guarantee** 

#### Evaluation

O Per-Flow FairnessDRFPS-PHUG

- 100 concurrent tenants
- 3000 machines with 3Tbps total capacity
- Original placement and communication patterns from the Facebook trace



**Isolation Guarantee** 



#### Bursty Demands

Periodic demand bursts in Spark streaming



#### Long-Term Guarantees

Predictable performance guarantees over time

# #**3**

## Decentralized Algorithms

Survive master failures and enable low response times

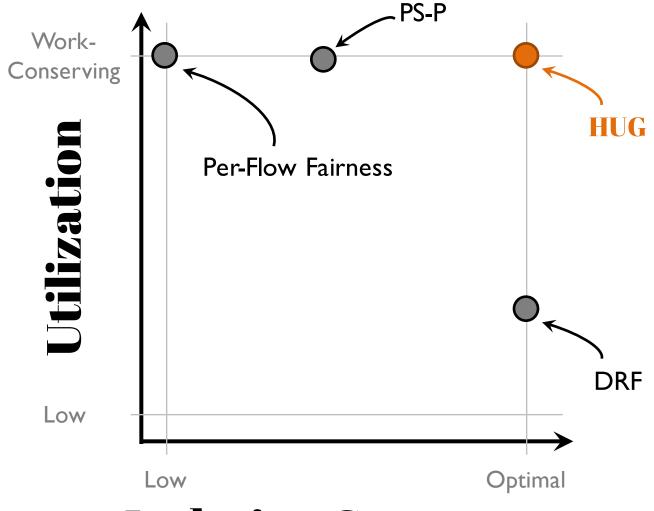


# Highest Utilization with the Optimal Isolation Guarantee

- Generalizes single- and multi-resource fairness schemes
- Optimal worst-case performance guarantees for tenants
- Highest utilization for operators

## HUG in Cooperative Setting

- 1. Optimal Isolation Guarantee
- 2. Work Conservation



**Isolation Guarantee** 

## Evaluation

A 3000-machine trace-driven simulation based on a snapshot of Facebook production trace

- I. Does it provide isolation guarantee?
- 2. Does it improve utilization?
- 3. Is it practical?



## Optimal Progress for ALL

	Per-Flow Fairness	PS-P <sup>2</sup>	DRF <sup>3</sup>	HUG
Max	1	1	0.74	0.74
Min	0.0001	0.10	0.74	0.74
Max-to-Min Progress Ratio	10000X	<b>10X</b>	<b>1X</b>	<b>1X</b>

<sup>1. 100</sup> tenants in this particular snapshot. The unit of progress is Gbps.

## Higher Network Utilization

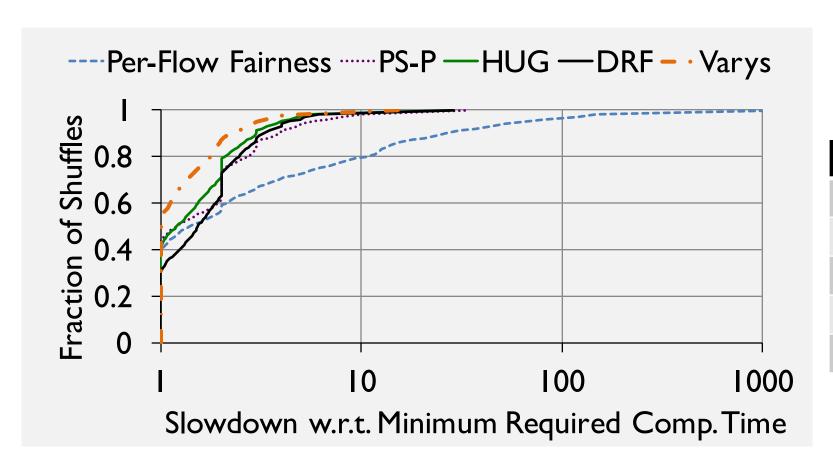
	Per-Flow Fairness	PS-P <sup>2</sup>	DRF <sup>3</sup>	HUG
Total Utilization (Tbps)	2.21	2.20	1.42	2.00
Max-to-Min Progress Ratio	10000X	10X	1X	<b>1X</b>

<sup>1. 100</sup> tenants in this particular snapshot. The unit of progress is Gbps.

<sup>2.</sup> FairCloud: Sharing the Network in Cloud Computing, SIGCOMM'12

<sup>3.</sup> Dominant Resource Fairness: Fair Allocation of Multiple Resource Types, NSDI'll

### Long-Term Performance



	Average Time
Per-flow Fairness	1.49X
PS-P	1.14X
DRF	1.14X
HUG	IX
Varys <sup>1</sup>	0.69X

## Coordination Overheads and Scalability

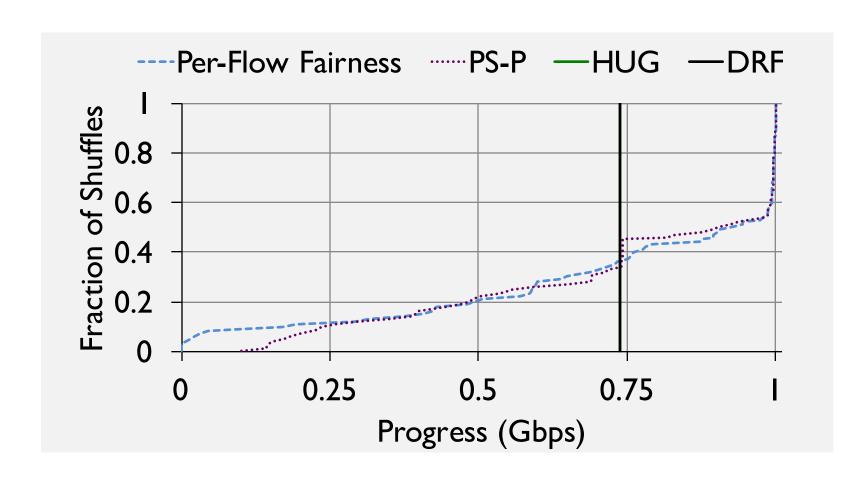
#### Computation overheads

- Less than 5 µs for 100machine cluster
- Less than 10 ms for 100,000 machines

#### Communication overheads

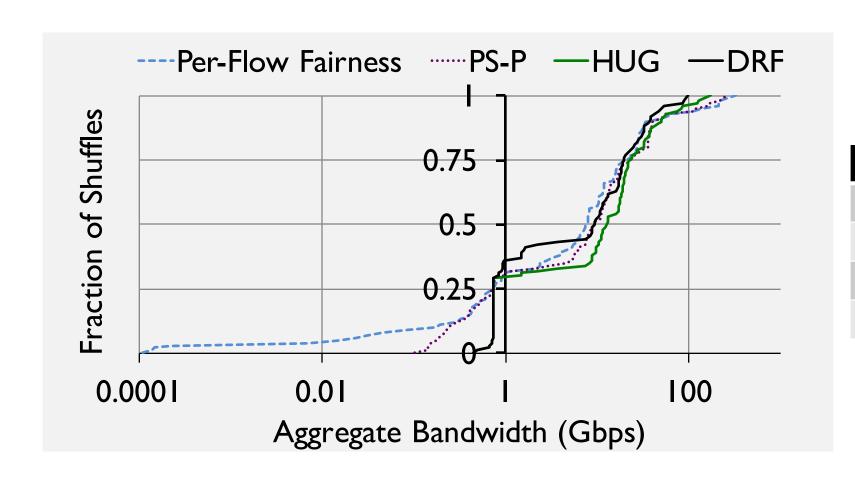
- Less than 10 ms for 100machine cluster
- Less than I second for 100,000 machines

## Optimal Progress for ALL



	Max/Min Ratio
Per-flow Fairness	10000X
PS-P	10X
DRF	IX
HUG	IX

## Higher Utilization



	Max/Min Ratio
Per-flow Fairness	3240000X
PS-P	2590X
DRF	196X
HUG	340X